# Feature Subset Selection Based on Bio-Inspired Algorithms\*

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Many feature subset selection algorithms have been proposed and discussed for years. However, the problem of finding the optimal feature subset from full data still remains to be a difficult problem. In this paper, we propose novel methods to find the relevant feature subset by using biologically-inspired algorithms such as Genetic Algorithm and Particle Swarm Optimization. We also propose a variant of the approach considering the significance of each feature. We verified the performance of the proposed methods by experiments with various real-world datasets. Our feature selection methods based on the biologically-inspired algorithms produced better performance than other methods in terms of the classification accuracy and the feature relevance. In particular, the modified method considering feature significance demonstrated even more improved performance.

*Keywords:* genetic algorithm, particle swarm optimization, feature redundancy and relevance, wrapper approach, inductive learning algorithm

# **1. INTRODUCTION**

Feature subset selection is about finding the optimal subset of features, among the full features, that renders the best performance in terms of well-defined criteria such as the classification accuracy in labeled data and the total cost associated with feature subsets [1-3]. The importance of feature selection in machine learning stems from its ability to improve such learning performance. In other words, through feature selection, we can reduce the cost of learning (both the acquisition cost/risk of feature values and the computational overhead in learning) and obtain higher classification accuracy, compared to the learning with the entire feature set.

In order to handle the inherent exponential complexity of the task (*i.e.* the existence of exponential number of candidate subsets), a number of approaches to feature subset selection have been proposed in the literature [1-21], which are based on diverse search strategies. (See [1-3, 9-12] for surveys.) First, an exhaustive search was employed to find the best feature subset under certain criteria [4, 5]. In this approach, the candidate feature subset is found using exhaustive search. However, exhaustive search is computationally infeasible in practice, except in those rare instances where the total number of features is quite small. Therefore, a number of researchers have explored the use of heuristics or randomized algorithms for feature subset) or eliminated (starting from the entire feature set) sequentially to determine the final feature subset [6-8]. Heuristics such as mu-

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Received December 7, 2009 revised March 29 & November 1, 2010; accepted December 15, 2010. Communicated by Chih-Jen Lin.

<sup>\*</sup> This paper was supported by the Special Research Grant of Sogang University to Jihoon Yang.

tual information, relevance, and relevance of each feature were also employed to find the optimal feature subset [13-17]. In addition, several authors explored the use of randomized population-based heuristic search techniques for feature subset selection [3, 18, 19].

Though each of the various approaches described above has its own rationale and criterion for finding quality feature subsets, it has demonstrated limited success and the feature subset selection still remains as a difficult task. Against this background, we aim to develop novel feature subset selection methods that produce quality solutions in terms of search criteria (*e.g.* classification accuracy, feature costs). More precisely, the new method combines biologically-inspired algorithms and well-defined heuristics expecting to inherit the merits of each approach, based on our previous experimental work on the task [20, 21].

Biologically-inspired (or bio-inspired in short) algorithms have been contrived based on the principles of the behavior of organisms, and applied to mainly optimization problems [22-26]. Among the various approaches, we consider two bio-inspired algorithms in this paper: Genetic Algorithm (GA) and Particle Swarm Optimization (PSO). GA is based on the survival of the fittest and tries to find the best solution through evolutionary processes of crossover and mutation among the individuals in the search space. PSO mimics the phenomenon of the swarm (or flocking) of creatures and attempts to find the best solution by changing the form of the swarm of individuals. As the bio-inspired algorithms are known to be generally quite effective for rapid global search of large search space in difficult optimization problems, we aim to combine the bio-inspired algorithms (as a wrapper defined in [3]) with inductive learning algorithms in a bid to find the optimal feature subset that yields the best performance. (See [27-29] for explanations on inductive learning algorithms.) Feature subset selection algorithms are said to follow a *filter* approach if feature selection is performed independently of the learning algorithm used, and said to follow a wrapper approach otherwise. In addition, we compare the performance of bio-inspired approaches to those of several state-of-the-art approaches, and finally propose new algorithms for feature subset selection. To this end, we combine the bio-inspired methods with the well-defined significance (or relevance) of each feature (by mRMR [13] as described in section 3) which was verified to be the best heuristic in [20, 21].

The rest of the paper is organized as follows: Section 2 briefly describes some of the characteristics that need to be considered in feature subset selection. Section 3 includes detailed descriptions on our approach that uses bio-inspired algorithms combined with inductive learning algorithms and the significance of a feature in subset selection. Section 4 explains the various real-world data and experimental setup designed to evaluate the performance of our approaches, followed by the results of experiments presented in section 5. Section 6 concludes with summary and discussion of some directions for future research.

# 2. CHARACTERISTICS OF FEATURE SUBSET SELECTION

Ideally, feature selection methods should choose the optimal feature subset from the candidates that best describes the target concept inherent in the data. The following aspects need to be considered in the process of feature selection.

#### 2.1 Starting Point

First, we must determine the starting point in the feature space and the direction of search. The search can start with no features (*i.e.* empty subset), and keep adding features in the subset. Or, it can start with all features (*i.e.* full subset), and keep eliminating features. The former is called *forward selection*, and the latter is known as *backward elimination* [3, 10]. Generalizing the idea of forward selection and backward elimination, we can start the search with any number and combination of features.

#### 2.2 Search Strategy

Theoretically, the best feature subset can be found by evaluating all the possible subsets. However, such an exhaustive search of the feature space needs to explore all of  $2^n$  possible subsets of *n* features, which is impractical for large number of features. Therefore, we have to resort to more realistic approaches. As described in section 1, a variety of approaches have been proposed for this purpose [1-21]. Though these approaches are practical, they are not guaranteed to find the optimal subset of features. This is natural because those approaches sacrifice the quality of the feature subset (to an acceptable degree) for the computational overhead (avoiding the exponential complexity). It is thus of importance to find a good algorithm considering this trade-off.

## 2.3 Subset Evaluation

After generating candidate feature subsets, we need to evaluate them. As aforementioned, a feature subset selection algorithm is termed either wrapper or filter approach by whether it makes use of a learning algorithm for evaluating feature subsets or not. In other words, the wrapper approach determines the goodness of a feature subset by applying it to a learning algorithm and evaluate the performance (*e.g.* by the classification accuracy). On the other hand, the filter approach evaluates features using some measures independent of the learning algorithm (*e.g.* mutual information [28], *mRMR* [13]).

## 2.4 Stopping Criteria

Finally, we must decide the criteria for halting the search. For example, we can stop adding or removing features when none of the alternatives improves the performance, or when the number of selected features reaches a pre-determined threshold [11]. We can then choose the best subset among the candidates we have encountered during the search.

## **3. BIO-INSPIRED APPROACHES TO FEATURE SUBSET SELECTION**

Feature subset selection is a hard task and not efficiently manageable when the dimensionality of the feature space is high. Bio-inspired algorithms are appropriate candidates to the task, producing quality solutions within reasonable amount of time and efforts. We propose wrapper-based approaches to feature subset selection based on two kinds of bio-inspired algorithms as described in this section.

#### **3.1 Bio-Inspired Algorithms**

Bio-inspired algorithms have been conceived based on the principles of the behavior or the phenomena in living organisms and creatures, such as gene evolution, insect swarming, bird swarming, food foraging, and the like [25]. Bio-inspired algorithms are wellknown for their applicability to optimization problems. Each individual in a bio-inspired algorithm represents a candidate solution to the problem, and the algorithm converges to the optimal solution (under certain assumptions) through the evolutionary interactions of the individuals in the solution space.

There exist a variety of bio-inspired algorithms [22-25], among which the *Genetic Algorithm* (GA), and the *Particle Swarm Optimization* (*PSO*) are considered in the paper. (Yet another popular bio-inspired algorithm, the Ant Colony Optimization (ACO) was experimentally proven to perform comparable to GA in our previous work [19] and is thus not considered in this paper.)

A fitness function is an objective function that quantifies the optimality of a solution (*i.e.* individual) in bio-inspired algorithms including *GA* and *PSO*. In this paper, the fitness function is defined by the accuracy of a learning algorithm. That is, each individual is evaluated by the learning accuracy based on the feature subset it represents. The bio-inspired algorithm attempts to find the best feature subset through evolution by wrapping the evaluation process of candidate solutions.

## 3.2 Feature Subset Selection using Genetic Algorithm (GAFSS)

The *Genetic Algorithm* (*GA*) is one of the bio-inspired algorithms using techniques inspired by evolutionary biology such as inheritance, mutation, selection, and crossover [23]. Typically, solutions (called individuals or *chromosomes*) are represented as strings in *GA*. The evolution starts from a population of randomly generated individuals and happens in generations. In each generation, the fitness of each individual is evaluated, and multiple individuals are stochastically selected from the current population based on their fitness, and modified to form a new population by genetic operations such as cross-over and mutation. The new population is then used in the next iteration of the algorithm. The algorithm terminates when either the maximum number of generations has been reached, or a satisfactory fitness level has been obtained for the population.

In our *GA*-based feature subset selection, each individual is represented as a binary string encoding a feature subset. If the data consist of N features, an individual will be an N-bit binary string. If a bit is 1 the feature is chosen in the feature subset; if 0 it is not. Each individual in the population is thus a candidate feature subset. The initial population, whose size is set to 40 in our experiments, consists of randomly generated such individuals. The selection, crossover, and mutation processes are implemented in a standard way of *GA* [23]. That is, a fitness-proportionate selection is used for choosing mating pairs of individuals; a single-point crossover was adopted for crossover operation with the probability of 0.6; and mutation operation was applied to flip each bit of an individual (*i.e.* either from 1 to 0 or from 0 to 1) with the probability of 0.03. The maximum number of generation was set to 20 in our experiments. The parameter settings were based on results of preliminary runs.

#### 3.3 Feature Subset Selection Using Particle Swarm Optimization (PSOFSS)

*Particle Swarm Optimization (PSO)* is a stochastic, population-based evolutionary algorithm introduced by Kennedy and Eberhart [22, 24]. Similar to *GA*, a population of individuals (or *particles*) is initialized as candidate solutions for a given problem in *PSO*. The particles iteratively evaluate the fitness of the candidate solutions and remember the *location* where they had their best fitness. The particle's best solution is called the *particle best (pbest)* or the *local best (lbest)*, and the best single solution among all of the particles is called the *global best (gbest)*. In the solution space, each particle makes suitable changes in its *position* and *velocity* iteratively with respect to the best solutions.

Let  $X_i^{(t)} = (x_{i1}, x_{i2}, x_{iD})$  be the position (vector) of particle *i* and  $V_i^{(t)} = (v_{i1}, v_{i2}, ..., v_{iD})$  be the velocity (vector) of particle *i* at time *t* in *D*-dimensional space, respectively. Then particle *i* changes its position and velocity iteratively as follows,

$$V_i^{(t)} = V_i^{(t-1)} + c_1(P_i - X_i^{(t-1)}) + c_2(P_g - X_i^{(t-1)})$$
(1)

$$X_i^{(t)} = X_i^{(t-1)} + V_i^{(t)}$$
<sup>(2)</sup>

where  $P_i = \{p_{i1}, p_{i2}, ..., p_{iD}\}$  is the *pbest* of particle *i*,  $P_g = \{p_{g1}, p_{g2}, ..., p_{gD}\}$  is the *gbest* of all particles, and  $c_1$  and  $c_2$  are *cognitive factors*, respectively. As the algorithm continues, the fitness of the global best solution keeps improving.

To handle the feature subset selection task with *PSO*, we followed the same approach that we used in *GA*. Like the chromosomes in *GA*, each particle in the swarm represents a candidate feature subset. We also define the position vector of a particle as a binary string and the fitness function as the accuracy of a learning algorithm.

Because of the binary values in the position vector of particles, we need to modify the operations (1) and (2) of *PSO* accordingly. We followed the modified *PSO* operations suggested by Kennedy and Eberhart [24]. Let  $x_{id}^{(t)}$  be the *d*th element of  $X_i^{(t)}$ . Then  $x_{id}^{(t)}$  changes its value to 0 or 1 iteratively as follows,

$$v_{id}^{(t)} = v_{id}^{(t-1)} + c_1(p_{id} - x_{id}^{(t-1)}) + c_2(p_{gd} - x_{id}^{(t-1)}),$$
(3)

$$s(v_{id}^{(t)}) = \frac{1}{1 + \exp(-v_{id}^{(t)})},$$
(4)

if 
$$\rho_{id} < s(v_{id}^{(t)})$$
, then  $x_{id}^{(t)} = 1$ ; else  $x_{id}^{(t)} = 0$ , (5)

where  $v_{id}^{(t)}$ ,  $p_{id}$  and  $p_{gd}$  are the *d*th elements of  $V_i^{(t)}$ ,  $P_i$  and  $P_g$  as defined previously,  $s(v_{id})$  is a *sigmoid function* to normalize the value of  $v_{id}$  into [0.0, 1.0], and  $\rho_{id}$  is a vector of random numbers drawn from a uniform distribution between 0.0 and 1.0. In these binary *PSO* operations, the velocity parameter  $v_{id}^{(t)}$  acts as an individual's disposition to make one or the other choice (*i.e.* to select the feature or not). If  $v_{id}^{(t)}$  is high ( $s(v_{id})$  is close to 1.0), the individual  $x_{id}^{(t)}$  is more likely to choose 1, and 0 otherwise.  $c_1$  and  $c_2$  are set to 2 in our experiments after some preliminary runs. In addition, the same parameter values for the population size and the number of generations of 40 and 20 were used for a fair comparison with *GAFSS*.

#### 3.4 Combining Feature Relevance with GAFSS and PSOFSS

We have explained *GAFSS* and *PSOFSS* feature subset selection methods as wrapper approaches with *GA* and *PSO*, respectively. *GAFSS* and *PSOFSS* simply rely on the classification accuracy (of a learning algorithm used in the wrapper) of candidate solutions during the process of evolution. While the accuracy is the appropriate criterion to be considered, the *relevance* (or *significance* or *goodness*) of each feature can provide additional information and thus help produce the best feature subset. For instance, one of such relevance measures, the *mutual information* describes how two features are related to each other [28]. The relevance measures are actually the ones that have been applied in filter approaches for feature subset selection [3]. Here, we extend *GAFSS* and *PSOFSS* by incorporating the relevance of features and modifying the evolution operators accordingly.

First, we need to determine the method for measuring the relevance of a feature. A variety of filter approaches have been proposed in the literature among which several methods were compared experimentally [3, 20, 21]. Based on the experimental results, we chose the *mRMR* method [13] that was based on mutual information and showed the best performance. The mutual information of two random variables is a quantity that measures their mutual dependence [27]. Generally, the mutual information of two discrete random variables *X* and *Y* is defined as:

$$I(X;Y) = \sum_{y \in Y} \sum_{x \in X} p(x,y) \log\left(\frac{p(x,y)}{p(x)p(y)}\right),\tag{6}$$

where p(x, y) is the joint probability distribution function of *X* and *Y*, and p(x) and p(y) are the marginal probability distribution functions of *X* and *Y*, respectively. Intuitively, the mutual information is to measure the information that *X* and *Y* share. In other words, it measures how much the knowledge on one variable reduces the uncertainty about the other.

In *mRMR*, the mutual information between a feature and a class is used as the *relevance* of the feature for the class. If there exist data *D* that consist of *N* features  $x_1, x_2, ..., x_N$  and a class *c*, then the relevance of feature  $x_n$  ( $1 \le n \le N$ ) is defined by the mutual information between feature  $x_n$  and the class *c*:

$$relevance(x_n) = I(x_n; c). \tag{7}$$

This reflects the dependency of feature  $x_n$  on the target class c. The feature  $x_i$  with the largest relevance has the largest dependency on the class.

*mRMR* also considers the mutual information between features as the *redundancy* of each feature. The redundancy of feature  $x_n$  in a feature subset *FS* is defined by following equation:

$$redundancy(x_n) = \frac{1}{|FS| - 1} \sum_{x_i \neq x_n, x_i \in FS} I(x_i; x_n).$$
(8)

This indicates the dependency of feature  $x_n$  with other features. For example, when two

features are highly dependent on each other, the class-discriminative power would not change much if one of them were removed. In this case, these two features are said to have high redundancy. We thus need to find features that have low redundancy in order to find mutually exclusive features.

The criterion combining above two conditions is called *Minimal-Redundancy and Maximal-Relevance* (*mRMR*) [13]. It means that the goodness of a feature becomes larger if the feature has lower redundancy and higher relevance. A feature with low redundancy and high relevance implies that the feature is mutually exclusive to other features and highly dependent on the target class. The *mRMR* measure of feature  $x_n$  is defined as:

$$mRMR(x_n) = relevance(x_n) - redundancy(x_n).$$
(9)

To set the relevance of each feature, we first measure the *mRMR* values of all features. We represent the *mRMR* values of features in  $D = \{x_1, x_2, ..., x_N\}$  as  $\{m_1, m_2, ..., m_N\}$ . Then we calculate the average  $(\overline{m})$  and the standard deviation (s) of the values as:

$$\overline{m} = \frac{1}{N} \sum_{i=1}^{N} m_i, \tag{10}$$

$$s = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (m_i - \overline{m})^2}.$$
(11)

Also, we divide the data *D* into three sets which satisfy  $D = D_1 \cup D_2 \cup D_3$ :

$$D_{1} = \left\{ x_{i} \mid m_{i} - \overline{m} > \frac{s}{2} \right\}, D_{2} = \left\{ x_{i} \mid -\frac{s}{2} \le m_{i} - \overline{m} \le \frac{s}{2} \right\}, D_{3} = \left\{ x_{i} \mid m_{i} - \overline{m} < -\frac{s}{2} \right\}.$$
(12)

This is to separate the features into three different categories: features with higher *mRMR* values are in  $D_1$ , lower *mRMR* values in  $D_3$ , and others in  $D_2$ . Choosing the half of the standard deviation as the threshold for this categorization of data is a simple heuristic determined based on results of several preliminary runs. Our approach to combine *GAF-SS* and *PSOFSS* with *mRMR* relevance measure is described in the remaining part of this section.

## 3.5 GAFSS + mRMR

*GAFSS* combined with *mRMR* (*GAFSS* + *mRMR*) is the same as simple *GAFSS* except the *mutation*. The mutation processes of *GAFSS* and *GAFSS* + *mRMR* are shown in Algorithms 1 and 2, respectively. (The overall description on *GAFSS* was given in section 3.2.)

In GAFSS + mRMR, the relevance of a feature is checked before performing the mutation operation. When the value of a bit is about to change from 1 to 0, the mutation is actually happening only if the corresponding feature is not in  $D_1$ . This means that the feature is not removed from the feature subset if it is presumed to be relevant (in terms of *mRMR*). Similarly, the mutation of a bit from 0 to 1 occurs only if the feature is not in  $D_3$ . This means that the feature is not added to the feature subset if it is presumed to be irre-

```
Algorithm 1: GAFSS
N: Size of population
n: Number of bits in an individual
G_1 = \{x_{i1}, x_{i2}, \dots, x_{in}\}: List of features (x_n = 0 or 1) for individual i
P_m: Probability of mutation (0 < P_m < 1)
/* Do Mutation */
For i = 1 to N
     For j = 1 to n
           get random value rand (0 < rand < 1)
           If (rand < P_m)
                If (x_{ij} == 0) then x_{ij} = 1
                Else If (x_{ij} == 1) then x_{ij} = 0
           End if
     End for
End for
. . .
```

```
Algorithm 2: GAFSS + mRMR
N: Size of population
n: Number of bits in an individual
G_1 = \{x_{i1}, x_{i2}, \dots, x_{in}\}: List of features (x_n = 0 or 1) for individual i
P_m: Probability of mutation (0 < P_m < 1)
/* Do Mutation */
For i = 1 to N
     For j = 1 to n
           get random value rand (0 < rand < 1)
           If (rand < P_m)
                If (x_{ij} == 0)
                      If (x_j \in D_3) then x_{ij} = 0
                      Else x_{ij} = 1
                Else If (x_{ij} == 1)
                      If (x_j \in D_1) then x_{ij} = 1
                      Else x_{ii} = 0
           End if
     End for
End for
```

levant. By combining *GAFSS* and *mRMR* in this fashion, we control the mutation process and attempt to include features of high significance and to exclude features of low significance, which could improve the performance of *GAFSS*.

# 3.6 PSOFSS + mRMR

Similar to GAFSS + mRMR, *PSOFSS* combined with *mRMR* (*PSOFSS* + *mRMR*) is the same as simple *PSOFSS* except the random process (Eq. (5)) which corresponds to the mutation step of *GAFSS* + *mRMR* in Algorithm 2. The basic operations of *PSOFSS* 

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and PSOFSS + mRMR (except the *pbest* and *gbest* determination steps) are shown in Algorithms 3 and 4, respectively. (The overall description on *PSOFSS* was given in section 3.3.)

Algorithm 3: PSOFSS N: Number of particles D: Number of bits in particle (number of full features) *T*: Number of iteration  $X_i^{(t)} = (x_{i1}^{(t)}, x_{i2}^{(t)}, \dots, x_{iD}^{(t)})$ : List of features  $(x_n = 0 \text{ or } 1)$  for particle *i*  $V_i^{(t)} = (v_{i1}^{(t)}, v_{i2}^{(t)}, \dots, v_{iD}^{(t)})$ : Velocity of *i*th particle at iteration *t*  $P_i = (p_{i1}, p_{i2}, \dots, p_{iD})$ : *pbest* of particle *i*  $P_g = (p_{g1}, p_{g2}, ..., p_{gD})$ : gbest  $c_1, c_2$ : cognitive parameters For t = 1 to TFor i = 1 to NFor d = 1 to D $\begin{aligned} v_{id}^{(t)} &= v_{id}^{(t-1)} + c_1(p_{id} - x_{id}^{(t-1)}) + c_2(p_{gd} - x_{id}^{(t-1)}) \\ s(v_{id}^{(t)}) &= \frac{1}{1 + \exp(-v_{id}^{(t)})} \end{aligned}$ Get random a value  $\rho_{id}$  ( $0.0 \le \rho_{id} \le 1.0$ ) If  $(\rho_{id} < s(v_{id}^{(t)}))$  then  $x_{id}^{(t)} = 1$ Else  $x_{id}^{(t)} = 0$ End for End for End for

Algorithm 4: *PSOFSS* + *mRMR N*: Number of particles *D*: Number of bits in particle (number of full features) *T*: Number of iteration  $X_i^{(t)} = (x_{i1}^{(t)}, x_{i2}^{(t)}, ..., x_{iD}^{(t)})$ : List of features  $(x_n = 0 \text{ or } 1)$  for particle *i*   $V_i^{(t)} = (v_{i1}^{(t)}, v_{i2}^{(t)}, ..., v_{iD}^{(t)})$ : Velocity of *i*th particle at iteration *t*   $P_i = (p_{i1}, p_{i2}, ..., p_{iD})$ : *pbest* of particle *i*   $P_g = (p_{g1}, p_{g2}, ..., p_{gD})$ : *gbest*   $c_1, c_2$ : cognitive parameters ... For t = 1 to *T* For t = 1 to *N* For d = 1 to *D*   $v_{id}^{(t)} = v_{id}^{(t-1)} + c_1(p_{id} - x_{id}^{(t-1)}) + c_2(p_{gd} - x_{id}^{(t-1)})$  $s(v_{id}^{(t)}) = \frac{1}{1 + \exp(-v_{id}^{(t)})}$ 

```
Get a random value \rho_{id} (0.0 \le \rho_{id} \le 1.0)

If (\rho_{id} < s(v_{id}^{(t)}))

If (x_d \in D_3) then x_{id}^{(t)} = 0

Else x_{id}^{(t)} = 1

Else

If (x_d \in D_1) then x_{id}^{(t)} = 1

Else x_{id}^{(t)} = 0

End if

End for

End for

End for
```

As shown in Algorithm 4, the relevance of a feature is checked if it is in  $D_1$  or  $D_3$  in *PSOFSS* + *mRMR*. When the value of a bit is to be set 1 (*i.e.* for high velocity), the relevance of the feature is checked to see if it is in  $D_3$ , in which case the value is set to 0. Similarly, when the value of a bit is to be set 0 (*i.e.* for low velocity), the relevance of the feature is checked to see if it is in  $D_1$ , in which case the value is set to 1. By following this method, we attempt to include features of high significance and to exclude features of low significance, which could improve the performance of *PSOFSS*.

## 4. EXPERIMENTS

# 4.1 Dataset

20 real-world datasets were used in our experiments. All the datasets are from the *UCI Machine Learning Repository* [30] and summarized in Table 1. Though some of the datasets consist of about 20 features, most of them have large number of features, so they are appropriate to the feature subset selection task. The datasets are also diverse in terms of the number of classes and samples, as well. (For detailed descriptions on each dataset, see [30].)

#### 4.2 Experimental Setup

Our experiments were conducted with three purposes. First, we compared the performance of *GAFSS* and *PSOFSS* with some of the existing feature subset selection methods. For this comparison, we chose the following five methods: *mRMR* [13], *Mutual Information Measurement (MI)* [28], *I-RELIEF* [14], *INTERACT* [16], *and PAM* [17]. These methods have been recently introduced and demonstrated as competitive feature subset selection methods. The five methods were used as a filter to inductive learning algorithms to construct the classifier. In other words, each method produced a feature subset based on its selection criterion that would be used in the learning algorithm (See the references and our previous publications [20, 21] for detailed descriptions on the selection methods and preliminary experimental results.) So we compared the performance of seven approaches (*i.e. GAFSS, PSOFSS, MI, mRMR, I-RELIEF, INTERACT, PAM*). We compared them in terms of the number of selected features and the classification ac-

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Name	Features	Classes	Samples										
Audiology	69	24	226										
Dermatology	33	6	366										
Musk	166	2	475										
Spambase	57	2	4601										
Arrhythmia	277	16	452										
Ionosphere	34	2	351										
Waveform	21	3	5000										
Sonar	60	2	208										
Image Segmentation	19	7	2310										
Flag	28	6	194										
Hepatitis	19	2	155										
Lung Cancer	56	3	32										
Promoter	56	2	106										
Splice	60	3	3190										
Optdigits	64	10	3823										
SpectF	44	2	267										
Connect-4	42	3	691										
Water Treatment	38	13	527										
Isolet	617	26	6236										
HDR Multifeature	649	10	2000										

Table 1. Datasets.

curacy with the feature subset. For the five filter approaches, we reorganized the datasets using selected (reduced) features by each method on which the learning algorithms were applied. The number of selected features for the filter approaches was determined as follows: For *MI*, *mRMR*, and *I-RELIEF*, features were added to the feature subset in an incremental way (starting from an empty set) with respect to their selection criteria and the best feature subset (with the highest classification accuracy) was produced; for *INTER-ACT* and *PAM*, features were selected as suggested by the authors in the references and available software. As mentioned earlier, we went through twenty iterations (*i.e.* generations) with forty individuals (*i.e.* chromosomes or particles) for the two bio-inspired approaches. This work is an extension of our previous research in [3, 19] where the former is a *GA*-based approach that is similar to *GAFSS*, and the latter is an ACO-based approach that produced fairly comparable performance to *GAFSS*. Note that the main contribution of this paper is the introduction of *GAFSS* + *mRMR* and *PSOFSS* + *mRMR* which are improvements over *GAFSS* and *PSOFSS*.

In the second experiment, we compared the performance of *GAFSS* and *PSOFSS* with their variants (*i.e. GAFSS* + *mRMR*, *PSOFSS* + *mRMR*). For the variants, the same number of iterations, the size of population, and other parameters were used as in *GAFSS* and *PSOFSS*. In addition to the feature subset size and the classification accuracy, we also compared the learning curves in this experiment. This is to check the evolution speed and to figure out how fast each approach converges to the best solution.

In the third experiment, we explored the effectiveness of our approaches in selecting an appropriate subset of relevant features in the presence of redundant or useless features so as to maximize the accuracy of the resulting classifiers. Since it is not so easy to judge the usefulness of the features in real-world datasets without domain knowledge, we chose one of the common artificial datasets, *parity* (3-bit and 6-bit), constructed as follows: The original features are replicated once (to introduce redundancy) thereby doubling the number of features. Then an additional set of irrelevant features are generated and are assignned random boolean values. For 3-bit parity, 100 7-bit random vectors were generated and augmented with the 6-bit vectors (corresponding to the original 3 bits plus and identical set of 3 bits). In the same way, 100 12-bit random vectors were generated and augmented with 12-bit vectors (6 original bits and 6 identical bits) for 6-bit parity.

We used Weka [31] for our experiments. Weka is a well-known open-source data mining software based on JAVA, equipped with a variety of machine learning algorithms. Among those algorithms [27-29], three popular ones are adopted in our experiments: Naïve Bayes (NB) [32], Decision Tree (C4.5) [33], and Support Vector Machines (SVM) [34] with linear kernel. (See the references for detailed descriptions on the algorithms.) We conducted 10-fold cross-validation in all experiments.

# **5. RESULTS**

#### 5.1 Comparison Between Bio-Inspired Methods and Existing Methods

First, we computed the classification accuracy of data with all features (*i.e.* full feature set) using the three learning algorithms. The results are shown in Table 2. Then we carried out feature subset selection on the datasets using the seven methods (shown in Tables 3-5 with the classification accuracy and the feature subset size), and compared their performance with the results in Table 2.

Name	Acc (NB)	Acc (C4.5)	Acc (SVM)
Audiology	73.45	77.88	81.86
Dermatology	97.54	90.98	95.36
Musk	73.68	78.95	82.74
Spambase	79.29	92.61	90.42
Arrhythmia	59.07	66.37	67.70
Ionosphere	84.62	88.60	89.17
Waveform	78.20	75.60	81.22
Sonar	65.38	69.23	73.56
Image Segmentation	79.87	87.84	85.80
Flag	56.19	70.62	64.43
Hepatitis	85.16	79.35	85.81
Lung Cancer	62.50	59.38	50.00
Promoter	82.08	82.08	82.08
Splice	91.25	92.60	84.55
Optdigits	91.66	89.62	98.14
SpectF	68.54	73.78	79.18
Connect-4	54.85	63.68	63.82
Water Treatment	74.76	70.02	78.75
Isolet	84.35	83.24	96.81
HDR Multifeature	95.35	94.60	98.40
Average	76.89	79.35	81.49

Table 2. Classification accuracies with all features (%).

NB	N	11	mR	MR	I-RE	LIEF	INTE	RACT	PA	М	GA	FSS	PSO	FSS
	Acc	#F	Acc	#F	Acc	#F	Acc	#F	Acc	#F	Acc	#F	Acc	#F
Audiology	75.7	21	75.7	21	75.2	45	72.6	21	74.8	39	76.6	39	78.3	36
Dermatology	98.4	23	98.6	24	98.1	24	97.3	18	97.5	33	<u>99.2</u>	25	<u>99.2</u>	15
Musk	76.8	55	80.2	80	75.4	69	71.6	16	75.4	61	79.6	66	<u>81.7</u>	74
Spambase	90.1	30	<u>90.4</u>	22	84.4	15	82.6	30	79.8	46	89.5	29	90.1	26
Arrhythmia	68.4	41	69.9	54	67.5	16	68.1	23	63.5	124	67.7	88	70.7	119
Ionosphere	89.2	13	90.3	12	88.6	18	88.3	18	85.5	24	91.0	15	<u>91.7</u>	16
Waveform	78.2	16	78.6	16	78.6	16	78.3	19	78.3	19	79.4	15	<u>79.5</u>	13
Sonar	69.7	6	<u>79.2</u>	9	74.5	17	69.2	17	70.2	8	75.5	25	76.9	15
Image Segmentation	80.8	13	82.4	6	81.3	17	82.6	13	80.7	12	<u>84.9</u>	9	<u>84.9</u>	10
Flag	68.0	6	69.6	4	69.6	4	58.3	9	56.2	16	70.6	11	72.2	14
Hepatitis	84.5	16	86.5	4	84.5	17	83.9	9	83.2	11	89.7	8	<u>90.3</u>	7
Lung Cancer	78.1	5	84.4	6	75.0	10	75.0	8	62.5	22	84.4	28	<u>87.5</u>	21
Promoter	91.5	23	<u>98.1</u>	40	<u>98.1</u>	38	89.6	13	85.9	30	92.5	33	94.3	27
Splice	<u>91.7</u>	43	91.7	31	91.7	53	91.0	31	91.4	57	91.4	33	91.6	38
Optdigits	91.6	63	92.4	45	92.5	45	91.6	21	92.3	47	92.7	36	<u>93.2</u>	33
SpectF	74.9	3	74.9	9	74.9	3	73.0	15	71.2	26	<u>79.4</u>	1	79.0	7
Connect-4	65.3	6	65.4	4	65.0	4	63.7	9	54.9	40	66.	12	<u>68.7</u>	11
Water Treatment	74.2	32	75.9	22	75.9	17	75.3	16	73.2	32	78.9	15	79.3	20
Isolet	84.4	357	82.6	495	Х	Х	85.3	57	84.7	594	89.1	284	<u>89.6</u>	284
HDR Multifeature	95.6	420	95.4	402	Х	Х	96.6	131	95.1	564	96.4	313	96.7	301
Average	81.4	-	83.1	-	80.6	-	79.7	-	77.8	-	83.7	-	84.8	_

Table 3. Classification accuracies of feature subset selection methods (%)-NB.

Table 4. Classification accuracies of feature subset selection methods (%)-C4.5.

C4.5	N	II	mRM	AR 🛛	I-RE	LIEF	INTE	RACT	PA	М	GA	FSS	PSC	PFSS
	Acc	#F	Acc	#F	Acc	#F	Acc	#F	Acc	#F	Acc	#F	Acc	#F
Audiology	77.9	21	77.9	21	77.9	26	77.9	21	77.9	39	78.3	33	<u>78.3</u>	41
Dermatology	93.2	22	92.9	23	92.9	23	92.4	18	91.0	33	<u>95.9</u>	11	<u>95.9</u>	19
Musk	82.7	89	82.7	76	83.2	131	77.1	16	81.1	61	84.0	84	<u>88.0</u>	79
Spambase	93.0	17	93.3	26	93.2	49	92.8	30	92.9	46	93.1	37	<u>93.8</u>	26
Arrhythmia	70.6	21	70.6	18	69.7	34	70.1	23	67.7	124	72.4	111	73.2	112
Ionosphere	89.2	28	89.7	27	88.6	18	86.9	18	88.6	24	<u>92.0</u>	14	91.2	15
Waveform	76.4	11	76.2	15	76.4	15	75.7	19	75.8	19	76.8	15	<u>77.6</u>	13
Sonar	78.4	11	80.3	8	74.5	3	76.4	17	71.2	8	78.9	23	<u>84.1</u>	24
Image Segmentation	88.1	14	88.1	14	88.1	14	87.8	13	87.7	12	88.1	14	88.2	11
Flag	73.2	3	73.7	6	73.2	8	73.7	9	73.2	16	73.7	9	74.2	12
Hepatitis	81.9	13	83.2	1	81.9	12	82.6	9	81.9	11	<u>85.8</u>	5	<u>85.8</u>	4
Lung Cancer	68.8	5	59.4	5	65.6	6	62.5	8	59.4	22	<u>71.9</u>	5	<u>71.9</u>	25
Promoter	87.7	4	100	38	100	38	83.0	13	72.6	30	86.8	12	86.8	25
Splice	94.4	12	94.4	13	94.5	14	93.2	31	92.7	57	94.5	33	<u>94.7</u>	27
Optdigits	89.8	60	89.7	56	89.6	53	89.8	21	89.4	47	90.0	33	<u>90.4</u>	35
SpectF	79.4	1	82.4	20	79.4	2	74.2	15	74.5	26	83.5	10	<u>86.1</u>	15
Connect-4	67.0	3	66.7	6	67.4	2	65.0	9	64.0	40	70.2	16	<u>70.3</u>	19
Water Treatment	71.2	36	72.3	24	73.4	11	68.9	16	66.8	32	72.9	19	<u>76.3</u>	19
Isolet	80.3	429	83.1	273	Х	Х	80.4	57	83.1	594	83.6	325	<u>84.6</u>	313
HDR Multifeature	94.1	458	94.9	55	Х	Х	93.7	131	93.8	564	96.4	312	<u>96.7</u>	320
Average	81.9	-	82.6	-	81.6	-	80.2	-	79.3	-	83.4	-	84.4	-

Tables 3-5 are with the NB, C4.5, and SVM algorithms, respectively. The highest classification accuracy is underlined and bold-faced for each dataset. Note that the X's in those tables are due to the limited capability of *I-RELIEF* in subset selection for high-

										-				
SVM	N	11	mR	MR	I-REI	JEF	INTE	RACT	PA	М	GA	FSS	PSO	FSS
5 V IVI	Acc	#F	Acc	#F	Acc	#F	Acc	#F	Acc	#F	Acc	#F	Acc	#F
Audiology	81.9	48	82.3	46	82.3	49	76.1	21	78.3	39	<u>85.8</u>	43	<u>85.8</u>	42
Dermatology	98.1	23	97.5	24	97.5	24	96.7	18	95.4	33	98.6	22	<u>98.9</u>	19
Musk	83.8	110	84.8	153	83.4	157	71.2	16	77.5	61	85.3	95	<u>85.9</u>	79
Spambase	90.4	54	<u>90.5</u>	54	<u>90.5</u>	56	88.4	30	89.9	46	90.1	44	90.4	36
Arrhythmia	70.8	30	71.5	27	71.2	45	69.7	23	69.5	124	73.0	133	74.3	128
Ionosphere	89.2	17	89.2	25	89.2	33	88.3	18	87.2	24	90.6	19	<u>92.3</u>	17
Waveform	81.4	18	81.6	19	81.6	18	81.4	19	81.4	19	81.4	19	<u>81.6</u>	18
Sonar	77.4	23	80.3	15	78.4	33	75.0	17	75.0	8	81.7	21	<u>84.6</u>	28
Image Segmentation	85.8	18	85.8	16	85.8	17	85.1	13	85.0	12	86.1	13	86.2	16
Flag	63.9	18	66.5	23	66.0	21	57.2	9	62.4	16	66.5	17	<u>69.1</u>	22
Hepatitis	83.9	15	85.2	13	83.9	9	84.5	9	82.6	11	88.4	9	<u>89.7</u>	13
Lung Cancer	75.0	7	78.1	38	81.3	25	65.6	8	75.0	22	78.1	26	87.5	18
Promoter	86.8	18	<u>100</u>	38	<u>100</u>	38	88.7	13	80.2	30	96.2	33	95.3	31
Splice	85.0	44	84.8	21	85.0	18	84.5	31	84.5	57	85.4	39	85.2	34
Optdigits	98.2	63	98.3	47	98.3	45	96.2	21	98.2	47	98.2	44	<u>98.3</u>	44
SpectF	<b>79.8</b>	36	<u>79.8</u>	38	79.4	1	79.4	15	79.4	26	79.4	1	79.4	8
Connect-4	64.7	1	64.7	5	64.7	3	64.3	9	63.8	40	<u>64.</u>	20	<u>64.8</u>	21
Water Treatment	78.8	36	79.1	36	78.6	26	73.4	16	76.3	32	79.5	26	<u>79.9</u>	27
Isolet	94.8	354	96.9	402	Х	Х	92.8	57	96.7	594	<u>96.8</u>	325	<u>96.8</u>	313
HDR Multifeature	98.5	460	98.5	410	Х	Х	98.5	131	98.3	564	99.1	312	<u>99.5</u>	320
Average	83.4		84.8	1	83.2	-	80.9	-	81.8	I	85.2	I	86.3	-

Table 5. Classification accuracies of feature subset selection methods (%) - SVM.

dimensional datasets like Isolet and HDR Multifeature.

As we can see from the tables, most of the methods produced better performance with a reduced feature set than with the full feature set, regardless of the learning algorithm. In particular, *GAFSS* and *PSOFSS* showed improved performance than filter approaches for most of the datasets. Furthermore, *PSOFSS* performed better than *GAFSS* for majority of the datasets with the three learning algorithms, producing higher average accuracy over all datasets. Therefore, we can conclude that our bio-inspired approaches, combined with popular learning algorithms, are very effective for feature subset selection, and *PSOFSS* is particularly the best approach for the task.

As far as the learning time, filter approaches were faster due to its non-iterative characteristic. Precisely, *GAFSS* and *PSOFSS* are slower than *mRMR* proportional to the size of the population and the number of generations (*e.g.*  $40 \times 20 = 800$  in our experiments). However, this problem can be mitigated by one-time, offline learning that selects the optimal feature subset with the best classification accuracy. In addition, the evolutionary approaches produced best solutions, swiftly converging to quality solutions in a small number of generations as shown in section 5.2. This verifies the practicality of our proposed approaches.

## 5.2 Comparison Between Bio-Inspired Methods and Their Variants

After the experiments were conducted under the same experimental setup as explained in section 4, the results of bio-inspired methods and their variants with mRMR are summarized in Tables 6-8 for the three learning algorithms. mRMR was chosen since its performance was either better than or comparable to other filter methods as shown Tables 3-5.

ND	GAF	SS	GAFSS -	+ mRMR	PSOF	FSS	PSOFSS +	mRMR
ND	Acc	#F	Acc	#F	Acc	#F	Acc	#F
Audiology	76.55	39	77.43	36	78.32	36	77.88	33
Dermatology	99.18	25	99.18	22	99.18	15	<u>99.45</u>	19
Musk	79.58	66	83.37	53	81.68	74	<u>84.00</u>	72
Spambase	89.52	29	89.11	30	90.11	26	<u>91.31</u>	21
Arrhythmia	67.70	88	<u>68.14</u>	99	69.69	119	72.35	95
Ionosphere	90.88	15	91.45	17	91.74	16	92.02	18
Waveform	79.36	15	79.14	17	79.48	13	79.48	16
Sonar	75.48	25	76.44	26	76.92	15	79.81	23
Image Segmentation	84.85	9	84.85	9	84.85	10	84.85	10
Flag	70.62	11	70.10	18	72.16	14	73.20	11
Hepatitis	89.68	8	89.68	8	90.32	7	90.32	10
Lung Cancer	84.38	28	84.38	21	87.50	21	<u>90.63</u>	25
Promoter	92.45	33	<u>93.40</u>	32	94.34	27	<u>95.28</u>	30
Splice	91.38	33	91.44	35	91.63	38	91.97	34
Optdigits	92.73	36	<u>93.60</u>	39	93.23	33	<u>93.70</u>	39
SpectF	79.40	1	79.40	1	79.03	7	79.40	10
Connect-4	66.71	12	66.70	11	68.74	11	69.03	11
Water Treatment	78.94	15	79.13	22	79.32	20	77.99	21
Isolet	89.10	284	89.57	321	89.64	284	89.64	297
HDR Multifeature	96.35	313	96.25	370	96.70	301	97.30	286
Average	83.74	_	84.14	_	84.73	_	85.48	_

Table 6. Performance comparison of *GAFSS* and *PSOFSS* with their variants-NB.

Table 7. Performance comparison of GAFSS and PSOFSS with their variants-C4.5.

C4 5	GAFS	S	GAFSS + n	nRMR	PSO	FSS	PSOFSS + mRMR		
C4.5	Acc	#F	Acc	#F	Acc	#F	Acc	#F	
Audiology	78.32	33	78.32	33	78.32	41	78.32	36	
Dermatology	95.90	11	95.90	14	95.90	19	95.90	15	
Musk	84.00	84	<u>85.26</u>	74	88.00	79	<u>89.26</u>	82	
Spambase	93.13	37	<u>93.70</u>	32	<u>93.81</u>	26	93.61	25	
Arrhythmia	72.35	111	72.35	126	73.23	112	73.23	118	
Ionosphere	92.02	14	92.02	11	91.17	15	<u>92.31</u>	8	
Waveform	76.84	15	76.84	12	77.64	13	77.64	13	
Sonar	78.85	23	78.85	23	84.13	24	84.13	27	
Image Segmentation	88.10	14	88.14	15	88.23	11	88.23	12	
Flag	73.71	9	74.23	6	74.23	12	75.26	13	
Hepatitis	<u>85.81</u>	5	84.52	5	85.81	4	85.81	6	
Lung Cancer	71.88	5	71.88	16	71.88	25	71.88	22	
Promoter	86.79	12	86.79	17	86.79	25	86.79	26	
Splice	<u>94.48</u>	33	93.98	32	<u>94.70</u>	27	94.61	22	
Optdigits	<u>90.03</u>	33	89.69	36	90.40	35	<u>91.43</u>	35	
SpectF	83.52	10	83.52	10	86.14	15	84.64	5	
Connect-4	70.19	16	70.62	20	70.33	19	70.62	19	
Water Treatment	72.87	19	73.06	21	76.28	19	74.95	20	
Isolet	83.55	325	85.55	321	84.56	313	86.57	310	
HDR Multifeature	96.40	312	<u>97.10</u>	385	96.65	320	96.65	340	
Average	83.44	-	83.62		84.41	-	84.59	_	

In most cases, the modified methods using mRMR produced higher learning accuracies than plain *GAFSS* and *PSOFSS*. And overall, *PSOFSS* + *mRMR* showed the best performance among all the methods we considered.

SVM	GAF	SS	GAFSS +	mRMR	PSOF	SS	PSOFSS -	+ mRMR
5 V WI	Acc	#F	Acc	#F	Acc	#F	Acc	#F
Audiology	85.84	43	85.84	43	85.84	42	87.15	39
Dermatology	98.63	22	<u>98.91</u>	18	98.91	19	98.91	17
Musk	85.26	95	85.05	97	85.89	79	85.89	86
Spambase	90.09	44	<u>90.39</u>	39	90.39	36	<u>90.48</u>	36
Arrhythmia	73.01	133	75.45	158	74.25	128	75.45	158
Ionosphere	<u>90.60</u>	19	90.31	17	92.31	17	91.45	15
Waveform	81.42	19	81.42	19	81.60	18	81.60	18
Sonar	81.73	21	<u>82.21</u>	26	84.62	28	83.65	31
Image Segmentation	86.10	13	86.10	17	86.15	16	86.15	14
Flag	66.49	17	<u>69.55</u>	15	69.07	22	71.65	17
Hepatitis	88.39	9	86.45	11	89.68	13	89.68	10
Lung Cancer	78.13	26	<u>84.38</u>	22	87.50	18	87.50	26
Promoter	96.23	33	93.40	32	95.28	31	95.28	35
Splice	85.36	39	85.36	33	85.17	34	85.30	31
Optdigits	98.17	44	98.22	42	98.33	44	<u>98.38</u>	47
SpectF	79.40	1	79.40	1	79.40	8	79.40	21
Connect-4	64.83	20	64.83	20	64.83	21	64.83	16
Water Treatment	79.51	27	80.08	27	79.89	27	<u>81.21</u>	24
Isolet	96.75	356	96.90	356	96.75	313	<u>97.43</u>	324
HDR Multifeature	99.10	315	99.45	315	99.53	320	99.53	325
Average	85.25	_	85.69	-	86.27	-	86.55	-

Table 8. Performance comparison of GAFSS and PSOFSS with their variant - SVM.

In addition to the analysis on the accuracy, we also compared the learning speed in order to see how fast the algorithm converges to the best solution. For *PSOFSS* and *PSOFSS* + *mRMR*, we chose four datasets and derived the learning curves (*i.e.* trace of the current best accuracy) as shown in Fig. 1. The graphs in Fig. 1 indicate that the accuracy of *PSOFSS* + *mRMR* increases faster than *PSOFSS*. This shows another merit of the modified method that it quickly finds the optimal feature subset.



Fig. 1. Comparisons of evolution speed between *PSOFSS* and *PSOFSS* + *mRMR*. The horizontal axis means the number of iterations, and the vertical axis indicates the learning accuracy (%).

#### **5.3 Quality of Feature Subsets**

Table 9 compares the performance of *mRMR* and *PSOFSS* + *mRMR* on the parity datasets (*#rel* means the number of relevant features in the selected subset of size *#F*). While the subsets produced by *mRMR* included irrelevant features which caused low classification accuracy, *PSOFSS* + *mRMR* successfully found appropriate sets of features with high accuracy. This demonstrates the outstanding capability of our approach in feature subset selection.

Dataset	Classifier	m	RMR	2	PSOFSS + mRMR				
Dataset	Classifier	Acc	#F	#rel	Acc	#F	#rel		
	NB	57.00	1	0	<u>59.00</u>	4	1		
3-bit Parity	C4.5	58.00	2	0	<u>93.00</u>	3	3		
	SVM	<u>57.00</u>	1	0	<u>57.00</u>	2	1		
6-bit Parity	NB	<u>54.69</u>	1	0	<u>54.69</u>	4	3		
	C4.5	56.25	12	4	<u>62.81</u>	7	3		
	SVM	54.69	1	0	55.00	6	4		

Table 9. Feature subset comparison of *mRMR* and *PSOFSS* + *mRMR*.

# 6. CONCLUSION AND FUTURE WORK

In this paper, we designed efficient methods, *GAFSS* and *PSOFSS*, for the feature subset selection task based on bio-inspired algorithms such as the genetic algorithm and the particle swarm optimization. We also proposed variants of those approaches considering the relevance of each feature, which produced novel algorithms called *GAFSS* + mRMR and PSOFSS + mRMR.

The performance of *GAFSS* and *PSOFSS* are experimentally verified to outperform other state-of-the-art feature selection methods in terms of the classification accuracy and the quality of the feature subsets. Furthermore, GAFSS + mRMR and PSOFSS + mRMR demonstrated more improved performance over GAFSS and PSOFSS making use of the relevance information, in terms of both the learning accuracy and the evolution speed. Extensive experiments on various real-world data concluded the best performance with PSOFSS + mRMR.

There are some avenues for future research. First, the relevance measure we considered in this paper is mRMR which maximizes the relevance and minimizes the redundancy of features using the mutual information criterion. Based on mRMR, the data is divided into three different subsets which affect the feature selection process. Further studies on this procedure can be pursued. Also, research on various relevance measures can lead to the improvement of current algorithms.

Second, we might need to consider more than a single criterion for the fitness function. For instance, we can consider the cost (or risk) associated with each feature as well, and attempt to minimize the total cost while maximizing the learning accuracy. This is basically multi-objective optimization, which occurs frequently in our daily lives (*e.g.* medical diagnosis). Solving a multi-objective optimization problem in the feature subset selection task using bio-inspired algorithms is clearly of interest. Third, we can apply our idea to other existing bio-inspired algorithms (*e.g.* Ant Colony Optimization (ACO) [24-26]) or develop new bio-inspired algorithms.

Fourth, we can develop hybrid approaches for the feature subset selection task. While the bio-inspired algorithms are very successful in finding good solutions, they may require quite amount of time for evolution. We might as well develop hybrid approaches (*e.g.* combining bio-inspired approaches with filter approaches or simple randomized search) to reduce the computational overhead.

Lastly, we can look into the feature subsets produced by different approaches and elicit the optimal subset by coalescing them based on the consensus among the approaches (*e.g.* ensemble learning).

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